







 $\#I/Os = O(\log_B N + occ/B).$ 

### Insertion in B-tree

#### · Insert(k, v)

- search for relevant leaf u and insert (k,v) in u.
- If u now contains B+1 elements:
  - split it into two leaves u' and u''.
  - update parent(u)
  - · If parent(u) now has degree B+1 recursively split it.
- · If root split: add a new root node with degree 2 (height of tree grows)

#### • Example. B= 5. Insert(24, v)

# 

## Insertion in B-tree

#### · Insert(k, v)

- search for relevant leaf u and insert (k,v) in u.
- If u now contains B+1 elements:
  - split it into two leaves u' and u''.
  - update parent(u)
  - · If parent(u) now has degree B+1 recursively split it.
- If root split: add a new root node with degree 2 (height of tree grows)

### • Example. B= 6. Insert(18, v)



### Insertion in B-tree

#### · Insert(k, v)

- search for relevant leaf u and insert (k,v) in u.
- · If u now contains B+1 elements:
- split it into two leaves u' and u''.
- update parent(u)
- · If parent(u) now has degree B+1 recursively split it.
- · If root split: add a new root node with degree 2 (height of tree grows)

#### • $\#I/Os = O(\log_B N)$

### Deletion in B-tree

#### · Delete(k)

- search for relevant leaf u and delete element with key k in u.
- If u now contains B/2 1 elements:
- merge u with its sibling u'. If this results in u containing more than B elements split it into two leaves.
- update parent(u)
- If parent(u) now has degree B/2 1 recursively merge it.
- If root has degree 1: delete root (height decreases)
- Example. B= 6. Delete(24)





### Deletion in B-tree

- search for relevant leaf u and delete element with key k in u.
- If u now contains B/2 1 elements:
- merge u with its sibling u'. If this results in u containing more than B elements split
- · If parent(u) now has degree B/2 1 recursively merge it.
- If root has degree 1: delete root (height decreases)
- **Example**. B= 6. Delete(18)

### **Deletion in B-tree**

#### · Delete(k)

- search for relevant leaf u and delete element with key k in u.
- · If u now contains B/2 1 elements:
  - merge u with its sibling u'. If this results in u containing more than B elements split it into two leaves.
  - · update parent(u)
- · If parent(u) now has degree B/2 1 recursively merge it.
- If root has degree 1: delete root (height decreases)





### Amortized updates in (a,b)trees

 If b ≥ 2a then the number of rebalancing operations caused by an update O(1/a) amortized

