## Run-length compressed suffix arrays

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## **References and Reading**

[1] Sections 11.1, 11.2 of: Navarro, Gonzalo. Compact data structures: A practical approach. Cambridge University Press, 2016.

## **Exercises**

**1 RLCSAs** Consider the string *L* on which the FM-index of section 11.2 is based. A well-known fact is that, if the input text *T* is very repetitive (i.e. the set of distinct substrings is small), then the number *r* of equal-letter runs in *L* is very small. For this reason, *r* is usually considered to be a good measure of repetitiveness of *T*.

- **1.1** Explain (informally) why this is true. Hint: think about the origin of L as the list of characters preceding sorted suffixes.
- **1.2** Find an infinite family of texts with this property: each *T* in the family has  $\Theta(|T|)$  equal-letter runs, but column *L* has  $r \in O(1)$  equal-letter runs.
- **1.3** Propose an implementation of a run-length FM-index (RLFMI) taking advantage of this source of compressibility (i.e. the index should take advantage of the fact that  $r \ll |T|$ ).
- **1.4** If *L* has *r* equal-letter runs, what can we say about  $\Psi$ ? Can  $\Psi$  be compressed similarly? Propose an implementation of a run-length compressed suffix array (RLCSA) taking advantage of this source of compressibility.
- **1.5** Suppose  $r \in \Theta(\sqrt{n})$ , where n = |T| (i.e. our text is polynomially compressible). How fast can we support locate queries on RLCSA/RLFMI indexes while using only O(r) words of space? (e.g. with the solutions of exercises 1.3, 1.4)